

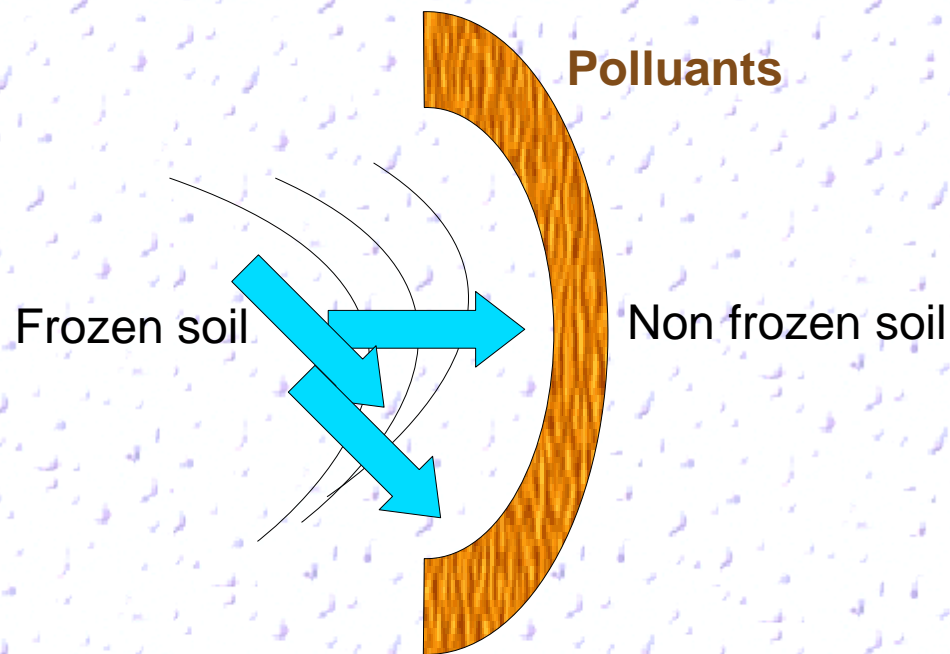
Water movements in frozen soils

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- Physical
- Chemical
- Biological
- ...
- Ventilation
- Biological treatment
- Thermal desorption
- ...

- Slow freezing
- Moving freezing front
- Displacement of impurities, pollutants
- Concentration of pollutants, impurities in reduced soil volumes



Heat and mass transfer : a complex problem

- Coupling between heat, dry air, vapor, water and ice
- Non linear equations
 - Conservation
 - Transport
- Huge number of state variables and equations (pde!)
- There is liquid water at temperature lower than 0°C
- Bad knowledge of the microscopical phenomena
- Many parameters value required (direct measurement not always possible or easy)

Hypothesis

- Local thermal, physical and chemical species and phases equilibrium
- Pores are spherical and are homogeneously filled by the ice
 - The behaviour of the frozen porous media is the one of a usual porous media whose porosity and permeabilities depend on the ice content
- Air and water vapor are perfect gas
- Transport is diffusive (Darcy, Fick)
- Non deformable porous dry soil

Model structure : three fluids and two solids model

- 5 species:
 - Liquid water
 - Water vapor
 - Ice
 - Solid dry soil
 - Dry air
- State variables
 - Liquid and gases: pressure, density, temperature
 - Ratio of frozen water
 - ...

Mass conservation for each specie i

$$\frac{\partial \rho_i}{\partial t} + \text{div}(w_i) = a_i$$

Water conservation

$$a_{el} + a_{es} + a_{eg} = 0$$

Energy conservation

$$\frac{\partial U}{\partial t} + \text{div}(h_a w_a + h_{eg} w_{eg} + h_{el} w_{el} + q) = 0$$

Energy balance

$$U = r_a u_a + r_{el} u_{el} + r_{eg} u_{eg} + r_{es} u_{es} + r_m u_m$$

Liquid water flow (Darcy)

$$w_{el} = \frac{w_{el}}{\rho_{el}} = -k_l \text{grad}(p_{el})$$

Water vapor and air flows (Darcy+Fick)

$$v_i = \frac{w_i}{\rho_i} = -k_g \text{grad}(p_g) - \frac{p_g}{p_i} D_f \text{grad}\left(\frac{p_i}{p_g}\right)$$

Conductive heat flux (Fourier)

$$q = -\lambda \text{grad}T$$

Air and water vapor are perfect gases

$$p_i = \frac{p_{i,g}}{M_i}$$

Thermodynamical gas-liquid equilibrium (Clapeyron)

$$p_{el} = p_{atm} + p_{el} \frac{RT}{M_e} \ln \left(\frac{p_{eg}}{p_{eg}^{sat}(T)} \right)$$

Mechanical gas-liquid equilibrium (Kelvin-Laplace + empirical)

$$s_l = \exp\left(\frac{p_c}{\rho_l g h}\right)$$

$$p_c = p_g - p_e' = 2\sigma(T)\gamma$$

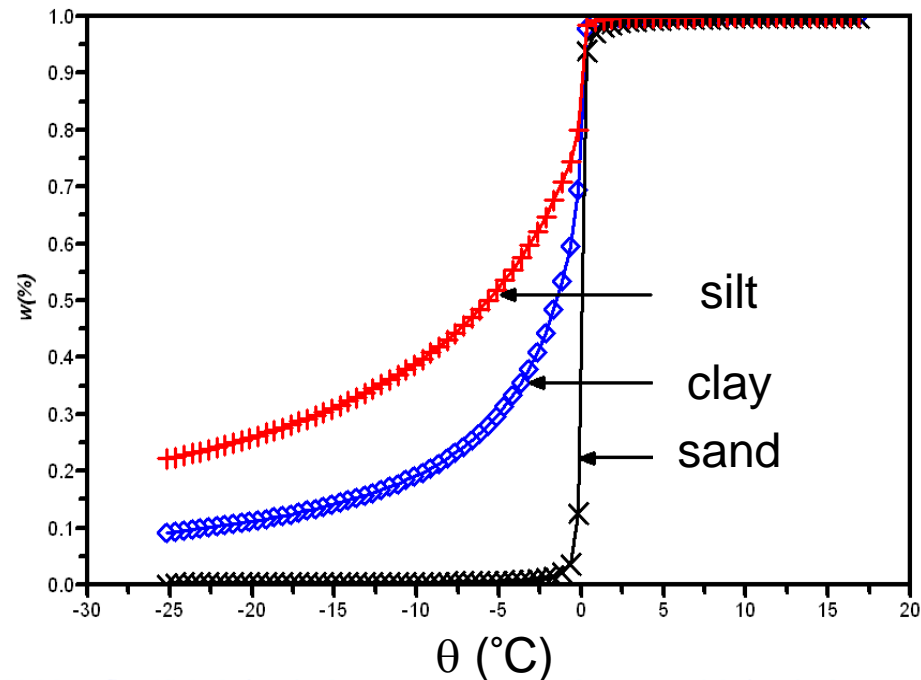
Ice content versus temperature (empi)

$$si\theta < 0 \text{ alors } \omega' = a e^{(\theta/c)}$$

$$si\theta > 0 \text{ alors } \omega' = b + (1 - b)(1 - e^{-\theta/c})$$

$$ou \theta = T - 273,15 \quad \omega' (\%)$$

Liquid water concentration in soils



Water superficial stress

$$\sigma = 0,2358(1 - T^*)^{1,256} \left(1 - 0,625(1 - T^*) \right) \left. \begin{array}{l} T^* = T/T_c \\ T_c = 647,096K \end{array} \right\}$$

Liquid and gas permeabilities

$$k_{rl} = \frac{k_{rl}}{k} \quad k_{rl} = \sqrt{S_l'} \left(1 - (1 - S_l'^{1/m})^m \right)^2$$

$$k_g = \frac{k_{rg}}{\mu_g} \quad k_{rg} = \sqrt{S_l'} (1 - S_l'^{1/m})^{2m}$$

Water vapor partial pressure

$$p_{reg}(T) = 68,148 - \frac{7214,64}{T} - 6,2973 \ln T$$

Equivalent conductivity

$$\lambda = \lambda_m^{1-\Phi} \lambda_{es}^{\Phi} \lambda_{el}^{\Phi} S_l'^{\Phi} \lambda_g^{\Phi} S_g'^{\Phi}$$

+ closing equation

Control volume method Scilab implementation

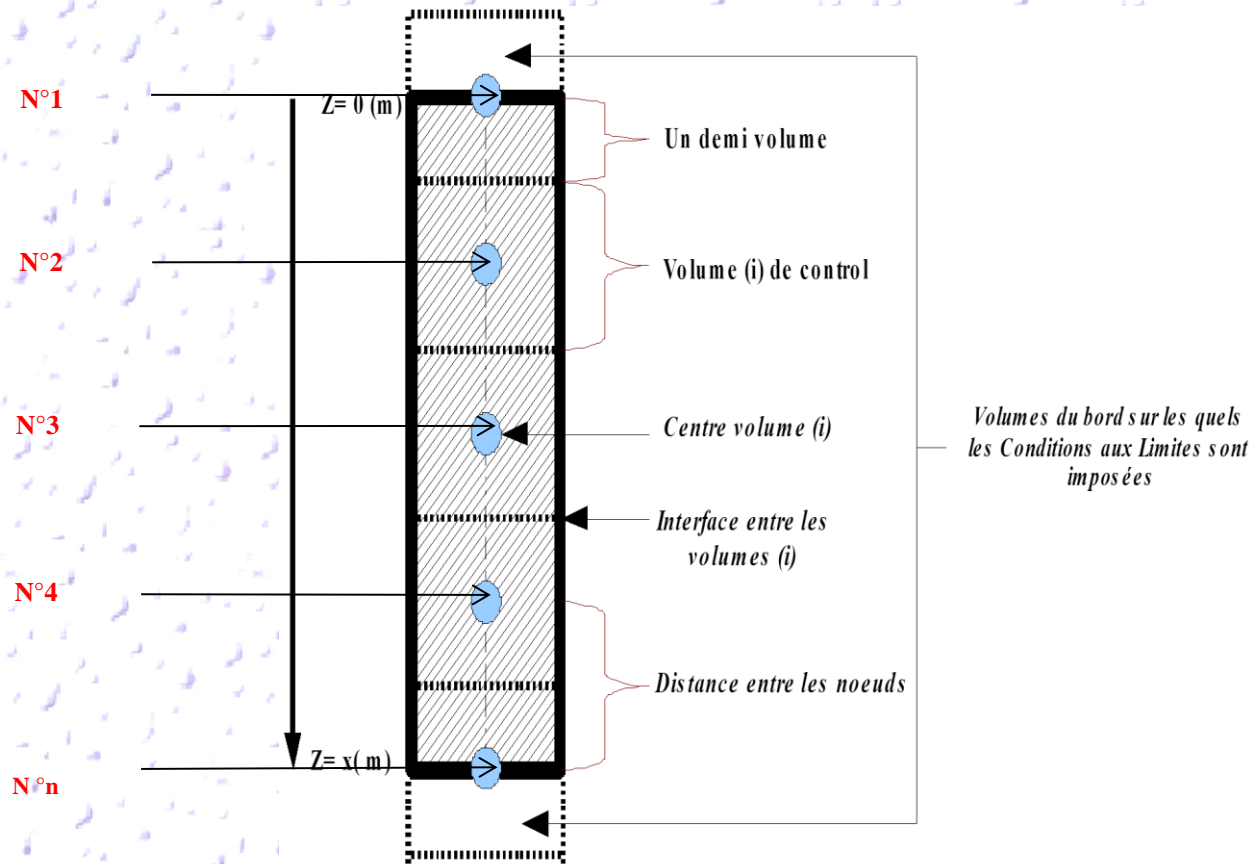


Figure (2) maillage uniforme

Homogeneous soil : clay

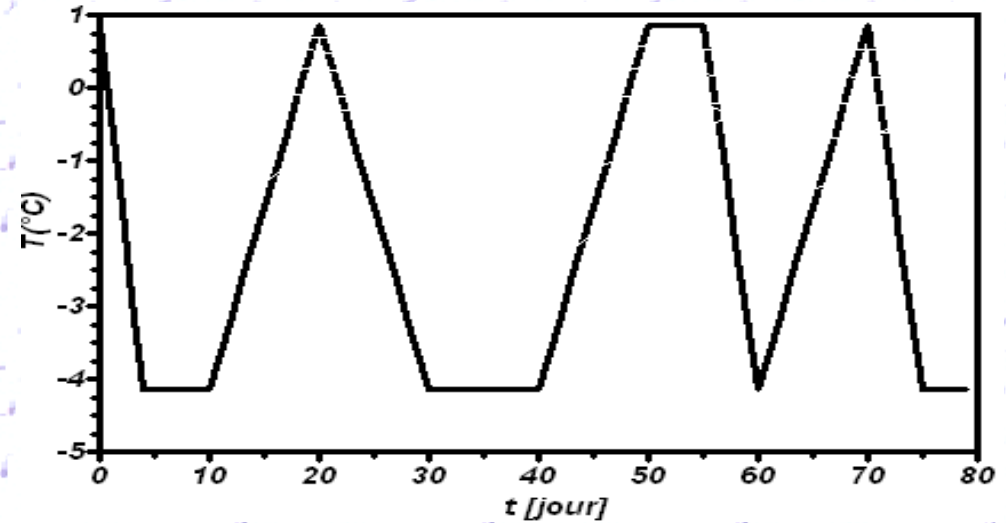
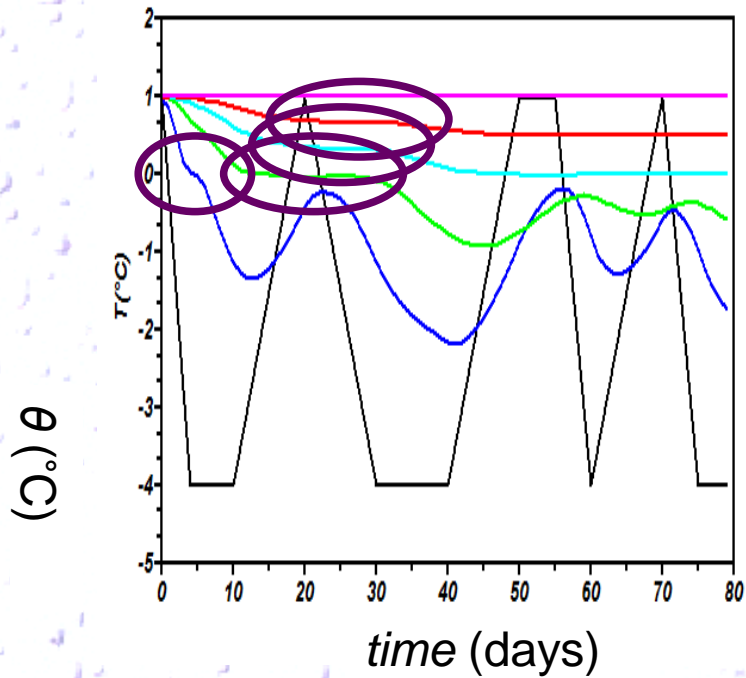


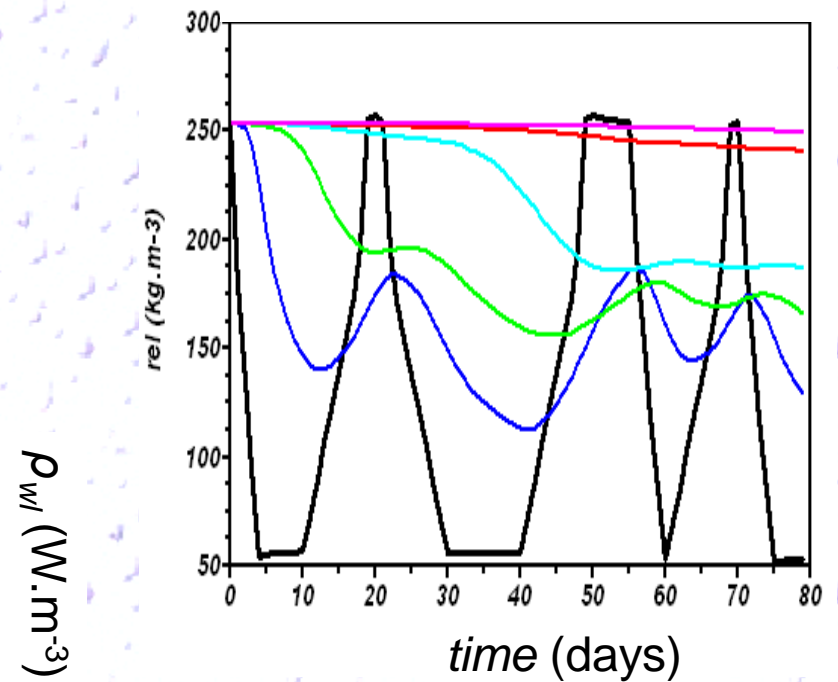
Figure (3) Evolution de la température imposée en surface du sol

- Top (node 1)
- 0.2m (node 3)
- 0.4m (node 5)
- 0.6m (node 7)
- 0.8m (node 9)
- 1 m (node 11)

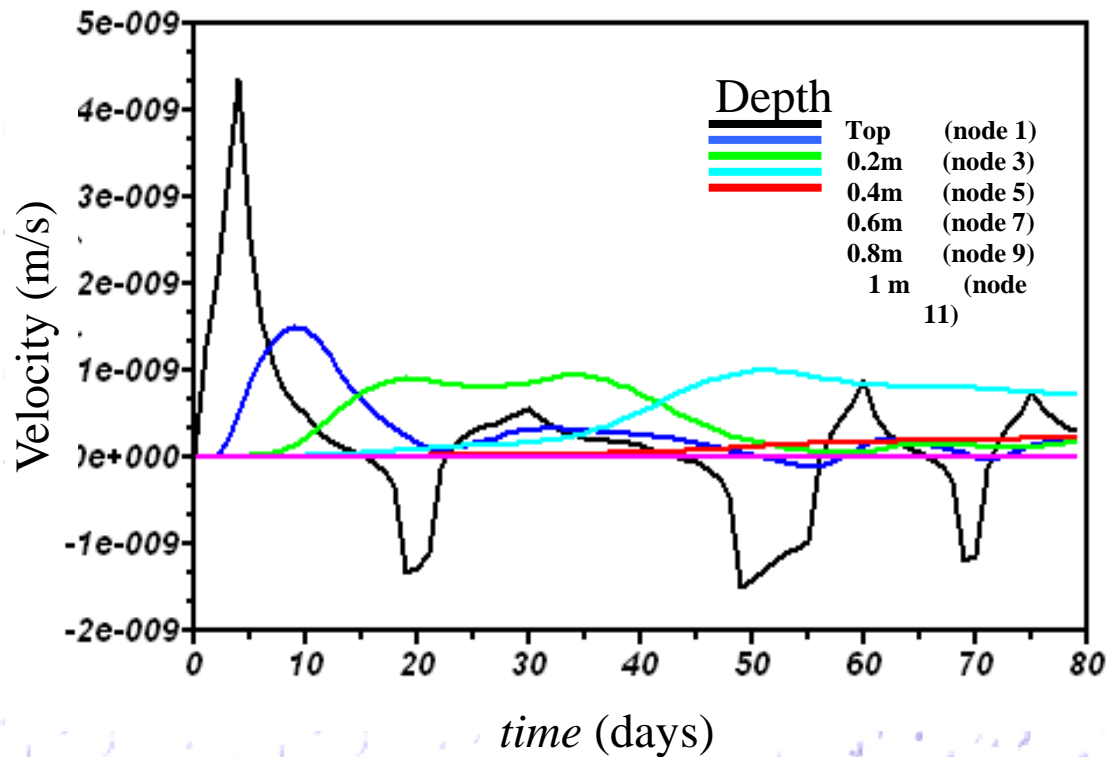
Soil temperature evolution



Liquid water apparent density evolution



Apparent liquid water velocity evolution



Bottom-up velocity

 $4.6 \cdot 10^{-9} \text{ m/s}$

Water flow

 $4.6 \cdot 10^{-9} \text{ (}$

Every day

 $0.4 \cdot 10^{-3} \text{ (}$

Every 5 days

 $2 \cdot 10^{-3} \text{ (}$

Top freezing

Top thawing

